

Exam in Soft Matter Physics TIF015/FIM110

Time and place: Saturday October 23, 14.00-18.00 2010.

Examiners: Aleksandar Matic (0730-346294), Johan Sjöström (0737279624)

Allowed material: Physics Handbook or equivalent, dictionary and pocket calculator

Grading: 24 points, is required for a passed.

Review of the exam: Contact Aleksandar Matic or Johan Sjöström after 6/11 2010

Note: All answers must be in English. Motivate all answers carefully. Answers without motivation give no credit.

1. The viscosity dependence of a glass forming liquid follows the Vogel-Fulcher-Tamman (VFT) equation, with the VFT-parameters $\eta_0=10^{-4}$ Pas, $B=12574$ K and $T_0=470$ K.

a) Give an order of magnitude estimate of the relaxation time for this liquid at 700 K. (6p)

b) What does the fragility of a liquid describe? (2p)

c) How, and why, does the glass transition temperature change when you change the cooling rate? (2p)

2. In a solution of the amphiphilic molecule sodium stearate (chemical formula $C_{18}H_{37} - COONa$) micelles are formed at sufficiently high concentrations.

a) Assuming that the critical chain length is given by $l_c \approx (0.154 + 0.1265n)$ nm, that hydrocarbon volume is given by $v \approx (27.4 + 26.9n) \times 10^{-3}$ nm³, and that the optimal head group area $a_0 = 0.7$ nm², determine the shape of the micelles. (4p)

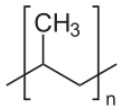
b) What do you expect can happen to the micelles and the solution if we add salt? (4p)

3. A colloidal suspension is formed by polystyrene spheres (radius 150 nm) dispersed in water. In a rheological experiment, at room temperature, the suspension is exposed to a strain rate $\dot{\gamma} = 500$ s⁻¹. Is this shear rate high enough to restructure the suspension? (6p)

A useful relation to use might be the Stokes-Einstein equation $D_{SE} = \frac{k_B T}{6\pi\eta a}$

4. Sketch how the strain rate (time derivative of strain) varies with the shear stress for a shear thickening liquid, a shear thinning liquid, and a Newtonian liquid. (3p)

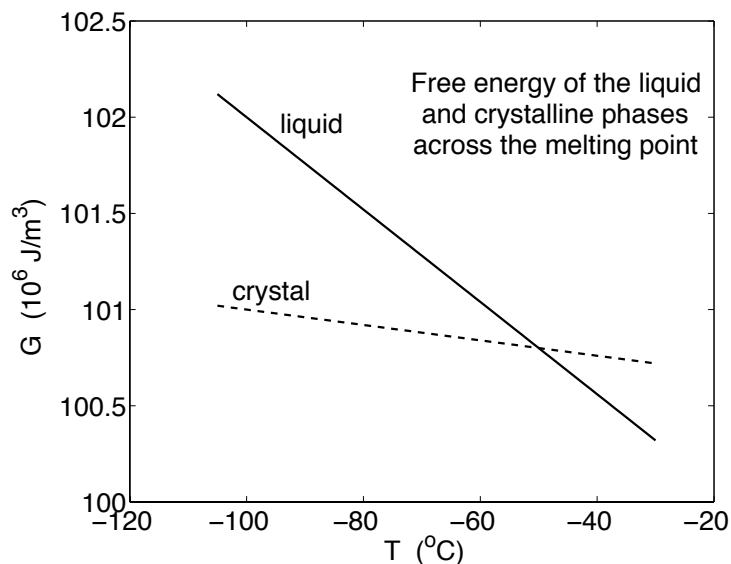
5. Consider a polymer of linear *atactic* polypropylene. The chemical structure is shown below:



At room temperature the melt is an amorphous rubbery material.

- If instead the polymer was *isotactic*, how would you expect the morphology (structure) of the polymer to change? (3p)
- The free energy, F , of a single polymer chain changes as a function of end-to-end distance, R , as $F(R) \propto R^2$.
What is the origin of this R -dependence of the free energy? (3p)
- If one polymer chain is instead isolated in vacuum the chain is stretched. Why is that and how does the free energy scale with R for this chain? (3p)
- We put the atactic polypropylene in a container of water. How would you expect the free energy to scale with R now? (3p)

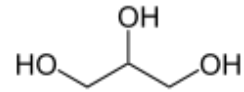
6. The figure below shows the free energy (per unit volume) of the liquid and crystalline phases above and below the melting point for a simple liquid. The metastable liquid is supercooled at $T = -100^\circ\text{C}$. Crystallization is thus governed by nucleation. The liquid-crystal surface tension is $\gamma \approx 5 \times 10^{-4} \text{ J/m}^2$.



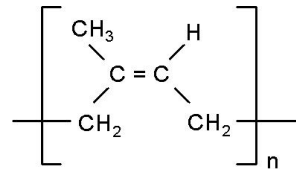
- At $T = 100 \text{ K}$, what is the critical nucleation radius? (4p)
- Is it likely that the liquid will crystallize at $T = -100^\circ\text{C}$? Don't forget to motivate! (3p)
- Is it likely that the liquid will crystallize $T = T_m - 0.1^\circ\text{C}$? Don't forget to motivate! (2p)
- What can you do to help the crystallization process at temperatures where nucleation is too slow? (2p)

7. Below you find the stress relaxation modulus (the stress after a sudden, constant strain) for the following materials:

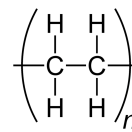
(i) Glycerol at $T=0\text{ }^{\circ}\text{C}$



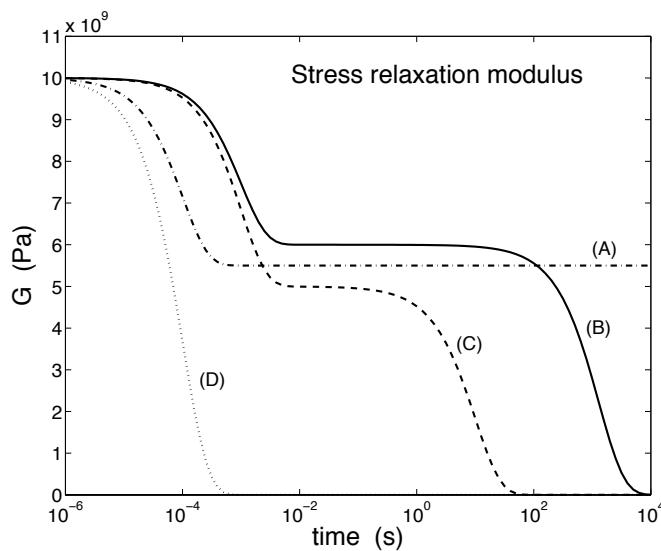
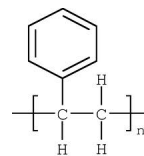
(ii) Vulcanized rubber at room temperature (crossed-linked polyisoprene of molecular weight 14000 g/mol).



(iii) Polyethylene with molecular weight 14000 g/mol at room temperature.



(iv) Polystyrene with molecular weight 14000 g/mol at $T=150\text{ }^{\circ}\text{C}$.



(a) Match the different curves (A-D) with the corresponding material (i-iv). **You must motivate each assignment in order to get credits!** (8p)

(b) From the figure, estimate the viscosity of glycerol at $T=0\text{ }^{\circ}\text{C}$! (2p)