

Department of Microtechnology and Nanoscience

## Wireless and Photonic System Engineering SSY085

2010-10-18, 14.00-18.00

Teachers in charge:

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Aids: Open book examination. Any printed material and calculator of choice is allowed. Communication devices (computers, mobile phones etc) are *not* allowed.

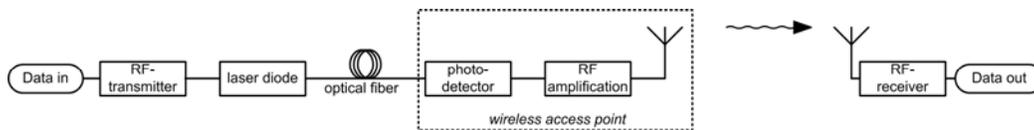
Examination checking: Friday Nov. 5<sup>th</sup>, 12<sup>00</sup> - 13<sup>00</sup> in room A604 at MC2

Convince yourself that you have understood the problem before you get started. Constructive and valuable gambits will also give points. If information is lacking in the description of the task, you must yourself introduce technical plausible assumptions. Make sure you clearly state such assumptions.

Grades: 3:  $\geq 24$ , 4:  $\geq 36$ , 5:  $\geq 48$

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1. Radio over Fiber (RoF) systems are often used to extend the coverage of wireless systems in dense areas with a lot of end users by connecting simple multiple wireless access points through a fiber link, as illustrated in the schematic below.



*Simple radio-over-fiber (RoF) downlink system.*

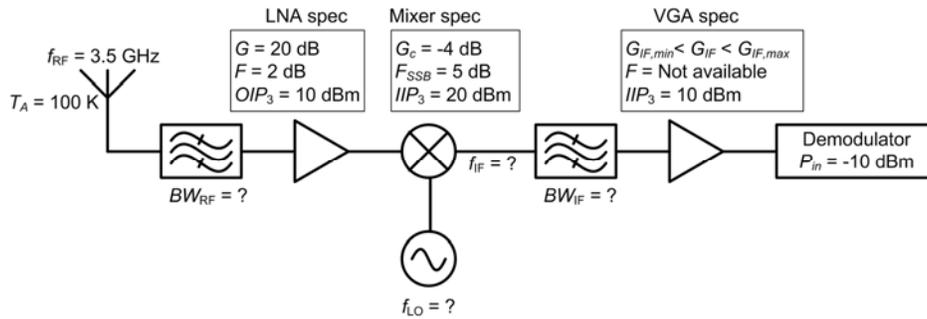
You should now use RoF technology to design a system for bi-directional distribution of mobile communication signals between one central unit and 10 wireless access points across the periphery of a large sports arena (500m  $\times$  500m).

The system should be designed to provide separate 5 MHz channels for up-link and down-link between each of the ten access points and the central unit. Regular mobile phones support the access points and need not to be included in the design.

To get full marks you must present block diagrams, component choices, and design calculations for the optical and microwave parts of the system. It is important to reduce the cost and energy consumption, so the power, amplification, and complexity in each block should be minimized. Use realistic assumptions where needed.

(30 points)

2. The figure below illustrates a 3.5 GHz super heterodyne receiver block diagram. The receiver will be used in an urban environment and should support a bitrate of 100 Mbit/s @ BER =  $10^{-5}$  using 64-QAM modulation format.



- Assign suitable values for the following parameters in the block diagram:  $f_{LO}$ ,  $f_{IF}$ ,  $BW_{IF}$ ,  $BW_{RF}$ . All values must be carefully motivated. (3p)
- Calculate the spurious free dynamic range of the receiver (you may assume lossless filters). Use this result to calculate the IF amplifier (VGA) gain variation required ( $G_{IF,min}$  and  $G_{IF,max}$ ) when the demodulator requires a fixed input power of 0 dBm. (4p)
- Estimate the ratio between the maximum and minimum range between the transmitter and the receiver ( $R_{max}/R_{min}$ ). The transmitter output power is fixed. (3p)

(10 points)

3. Multi-channel transmitters can be used reduce cost in cellular wireless systems. You should now consider a cellular wireless system in dense urban area with the following specifications:

Bitrate/channel: 10 Mbps (QPSK), BER <  $10^{-5}$   
 Outage probability: <5%  
 Receiver noise figure: 5 dB

How many channels can a single 1 GHz base station serve within a cell radius of 1 km if the total transmitted power is limited to 100 W? You may assume a base station antenna gain of 15 dB at a height of 20 m.

(10 points)

4. A 40 Gb/s OOK optical signal should be transmitted over an SMF with a loss of 0.2 dB/km. The transmitter supplies 0 dBm of (average) power. The receiver consists of a pin diode with responsivity  $R=0.8$  A/W, and you require a BER <  $10^{-9}$ . What is the attenuation-limited distance if you use

- no optical amplifiers at all, (5p)
- a preamplified receiver, where an EDFA with a gain of 20 dB and a noise figure of 6 dB is used directly before the detector? (5p)

(10 points)

## Solutions

Please note that these are our suggested solutions. Other solutions could be as good or better.

### Solution to 2a.

**BWIF:**  $R_b/(\text{spectral eff}) = 100\text{e}6/\log_2(64) = 16 \text{ MHz} \rightarrow$  Choose **BWIF = 20 MHz**

**BWRF:** Practical RF filters have bandwidths  $>\sim 5\%$ . Choose **BWRF = 5%\*fRF = 175 MHz**

**fIF:** The RF filter should block the image frequency, which is located at  $2*fIF$  from fRF. If the RF filter is centered at 3.5 GHz, this means that  $2*fIF > BWRF/2 \rightarrow fIF > BWRF/4 = 175 \text{ MHz}/4 = \text{ca } 45 \text{ MHz}$ . To keep some margin, we choose **fIF = 90 MHz**.

This margin will also make sure that reverse leakage of the LO frequency through the mixer and LNA is blocked and not radiated back from the antenna.

**fLO:** The local oscillator frequency is selected as the difference between fIF and fRF = 3.5 GHz +/- 90 MHz. We choose **fLO = 3.41 GHz**.

### Solution to 2b

% Solution presented as MatLab code

clear;

clc

%DRf = (P3/(No\*SNR))^(2/3) is the equation we will use to calculate DRf. We

%start out by findind No, SNR, and P3.

% RF filter

T1=0; %K Filter temp outside band.

% LNA

G2 = 100; % 20 dB

F2 = 10^-.2; % 2 dB

P3\_2 = 1e-2; % 10 dBm

T2 = (F2-1)\*290; %

% Mixer

G3 = 10^-.4; % -4 dB

F3 = 10^-.5; % 5 dB

P3\_3 = 0.1\*G3; % 20 dBm - 4dB (to get OIP3)

T3 = (F3-2)\*290;% 337 K SSD noise temp

% VGA

GIF = 10; %(DRf will actually not depend on GIF)

P3\_IF = 10^-2\*GIF; % 10 dBm + GIF (to get OIP3)

%The IF amp. is considered noiseless.

% Filters have very high IP3 and do not need to be included in the IP3

% calculations

P3 = (1/(P3\_2\*G3\*GIF) + 1/(P3\_3\*GIF) + 1/(P3\_IF))^(-1); %=0.0027\*GIF

P3\_dbm = 10\*log10(P3/1e-3)

% We need to have an SNR of 17.8 dB + 10\*log10(6) dB (17.8 dB from % eb/n0 and the factor 6 from spectral efficiency of QAM-64), se

Table 9.5 in Pozar

SNR\_db = 17.8 + 10\*log10(6)

SNR=10^(SNR\_db/10);

Ta = 100;

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B = 100e6/6; % B = Rb/spectral eff = 100 Mbit/s * 1/6 =16.7 MHz.
% Total noise power at receiver output:
No = 1.38e-23*17e6*((Ta + T2)*(G2*G3*GIF) + T3*(G3*GIF) + (T1 +
T2)*(G2*G3*GIF))
%(Which part is from the image frequency?)
%=6.84e-12*GIF

% Finally, the dynamic range calculation 3.108 in Pozar. Here GIF
will
% cancel out.
DRf = (P3/(No*SNR))^(2/3);
DRf_db = 10*log10(DRf)
%42 dB

% This yields the following VGA gain range:
% Min power at input of VGA = No/GIF
% Power at VGA output = -10 dBm

Gain_max_db = -10 - 10*log10(No/GIF*1000) - SNR_db
%48 dB
Gain_min_db = Gain_max_db - DRf_db
%6 dB

% Assume propagation constant = 3
rmax_rmin = 10^(DRf_db/10/3)
%25
return

```

### **Solution to 3**

```

% Solution presented as MatLab code
% Use the Hata-Okumura propagation model with the following
parameters
d = 1; % Cell radius
f = 1000; % Frequency
hb = 20; % Base station antenna height
hm = 2; % Mobile phone height

ch=0.8+(1.1*log10(f)-0.7)*hm-1.56*log10(f);
Lu_db = 69.55+26.16*log10(f)-13.82*log10(hb)-ch+(44.9-
6.55*log10(hb))*log10(d)

Ptx_dbm = 50; % Transmit power = 100W
Gtx_db = 15; % Transmit antenna gain

N0_dbm = 10*log10(1.38e-23*290*5e6*10^.5/1e-3) % Noise power at
receiver input (assume unity receive antenna gain for mobile)

snr_db = 9.6 + 3; % SNR = eb/no*Rb/B for QPSK modulation

out_marg_db = -10*log10(-log(1-.05)) % Outage probability margin
assuming Rayleigh fading environment (reasonable from the text, where
"dense" urban is stated.). prob_outage = 1-exp(-Pthr/P0), where P0 is
the nominal received power.

margin_per_user = Ptx_dbm + Gtx_db - Lu_db - N0_dbm - snr_db -
out_marg_db; % dB of margin per user

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$N = 10^{(\text{margin\_per\_user}/10)}$  % Use the margin to support N users

**N = 18 users**

#### **Solution to 4**

a)

This will be a thermal-noise-limited link, and the receiver sensitivity  $P_{\text{rec}}$  is obtained from  $Q=6$ , where  $Q=I_1/(2 \sigma_T)=2R P_{\text{rec}}/(2 \sigma_T)=6$ . In this case,  $\sigma_T^2=4k_B T \Delta f /R_L = 1.32e-11 \text{ A}^2$ , from which we get  $P_{\text{rec}}=6 \sigma_T /R=6(4k_B T \Delta f /R_L)^{1/2}/R=-18.7 \text{ dBm}$ . The allowed losses are thus 18.7 dB which corresponds to a link length of  $18.7/0.2=93.5 \text{ km}$ .

b)

Here signal-spontaneous noise will likely limit the link, and using  $P_{\text{rec}}$  to denote the average power in to the amplifier, the  $Q$  becomes  $Q=I_1/\sigma_{s\text{-sp}}=2RGP_{\text{rec}}/(4 R^2 GP_{\text{rec}} S_{\text{sp}} \Delta f)^{1/2}=(P_{\text{rec}}/(F_n h \nu \Delta f/2))^{1/2} = 6$ , from which we find the sensitivity to be

$$P_{\text{rec}}=18 F_n h \nu \Delta f.$$

By using  $F_n=4$ ,  $h \nu \Delta f=5.12e-9 \text{ W}$ , we get  $P_{\text{rec}}=-34.3 \text{ dBm}$ , and the corresponding fiber length  $34.3/0.2=171 \text{ km}$ .

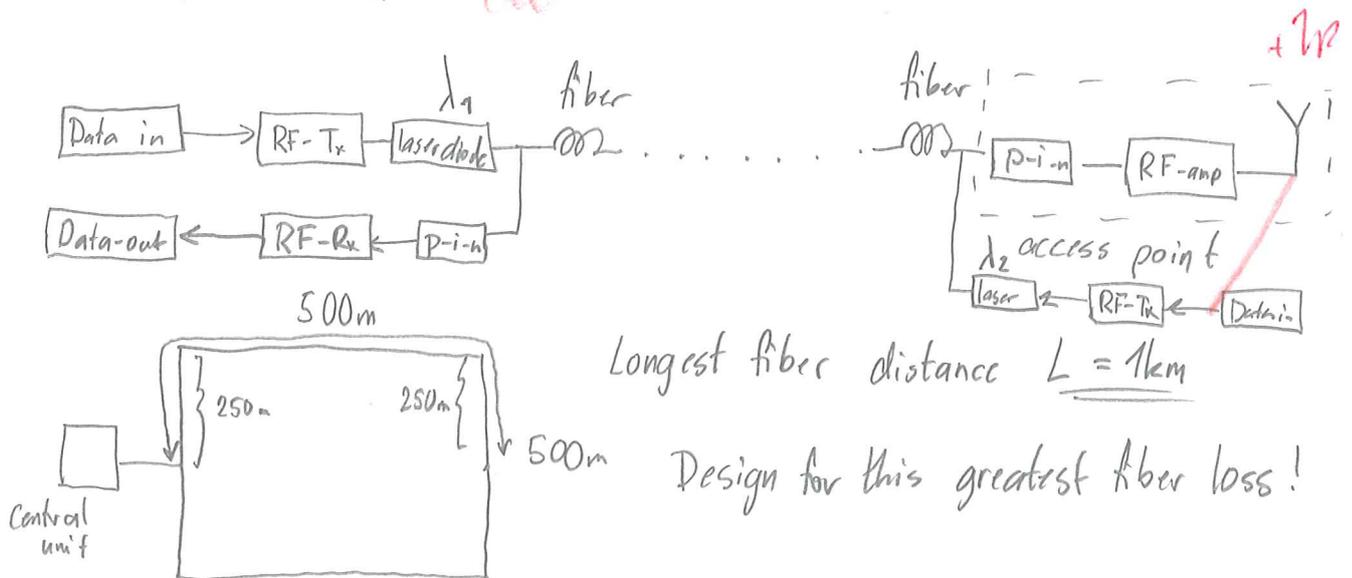
Check of noise powers: The s-sp noise power is  $\sigma_{s\text{-sp}}^2=4 R^2 F_n h \nu \Delta f P_{\text{rec}} G^2/2 = (6R F_n h \nu \Delta f G)^2=9.66e-11$ , which is almost 6 times the thermal noise, i.e. thermal noise is not completely negligible...

A more exact treatment accounts for the thermal noise as well in the expression for the  $Q$ , and can be shown to give

$$P_{\text{rec}}=18 F_n h \nu \Delta f + 6 \sigma_T / (RG) = -33.0 \text{ dBm}, \text{ and the distance is then } 165 \text{ km}.$$

1. The access points are spread across the arena periphery.  
 I assume that each wireless access point is connected to the central unit with an own fiber, down-link and up-link are transmitted over the same fiber using different frequencies for data from/to central unit.

The frequencies/modulation scheme are decided when designing the RF-transmitter. The fiber part is just making a link budget with RoF instead of free-space propagation model from the central unit to the access point.  $\lambda_1$  used for uplink,  $\lambda_2$  for downlink. I design with one RoF link for each wireless access point <sup>ok</sup> that is the system below is used 10 times, one for each access point at the arena. <sup>decided by lasers</sup>



The frequency used for the design is  $f = 900$  MHz (downlink) (for mobile phone users) <sup>ok</sup>  $f = 850$  MHz (uplink).  
 Each access point uses 5 MHz bandwidth for uplink/downlink.

Downlink

First I need an estimate of how much power needs to be transmitted at the access point antenna.

A mobile user is say at maximum  $R=100\text{m}$  from the access point and the receiver needs a minimum amount of power.

Assume QPSK is used with  $\text{BER} = 10^{-5}$   $\frac{E_b}{n_0} = 9,12$

$\Rightarrow \text{SNR} = 18,24$  needed | Data rate to mobile phone call  
 $= 12,6\text{dB}$   $R_b = 50\text{kbits/s} \Rightarrow B = 100\text{kHz}$

If mobile phone antenna  $T_A = T_o = 290\text{K}$  and noise figure of mobile phone receiver  $F = 3\text{dB} = 2$

$\Rightarrow \text{Noise power} = 10 \log(kT_o BF \cdot 1000) = -121\text{dBm}$

Minimum received signal level  $-108\text{dBm} = 1,58 \cdot 10^{-14}\text{W}$

(antenna in mobile phone has gain  $G_r \approx 1$ )

Using modified Friis equation with  $N = 2,5$   $R_o = 1\text{m}$

gives path loss  $10 \log\left(\frac{\lambda^2}{(4\pi R_o)^2} \frac{1}{(R/R_o)^N}\right) = -81\text{dB}$

$f = 900\text{MHz} \Rightarrow \lambda = 0,33\text{m}$

Add to this a fade margin of  $20\text{dB}$  (very many reflections inside arena)

yields total losses  $-101\text{dB}$

EIRP for antenna at access point  $-20\text{dBm}$

with omnidirectional antenna  $P_t = -25\text{dBm}$

$G_t = 5\text{dB}$

This we need after the fiber!

Since RF-amp. in accesspoint say  $G = 20\text{dB} \Rightarrow P_{\text{out}} = -45\text{dBm} = 3,16 \cdot 10^{-8}\text{W}$

from fiber link

RoF link

$P_{out} = P_{in} S_e^2 \alpha^2 R^2$  2p

assume  $R = 50 \Omega$  *no R is responsivity!*

Fiber used is MMF with  $\alpha = 1 \text{ dB/km}$  *linear scale loss*

Optical losses in 1km is 1dB  $\Rightarrow \alpha = 0,8$  above 1p

Photo detector used is InGaAs with quantum efficiency  $\eta = 0,8$  2p

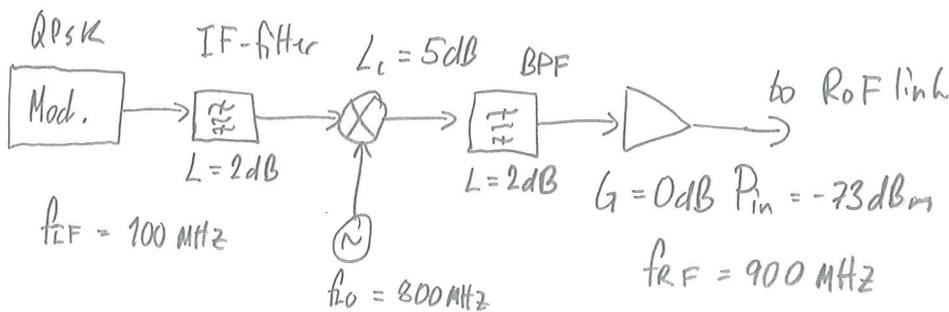
The laser used is of wavelength 1550nm (for downlink) 1p

$\Rightarrow$  Slope efficiency  $S_e = \eta \frac{h\nu}{q} = 0,64 \text{ W/A}$  1p

With  $P_{out}$  calculated  $P_{in} = \frac{P_{out}}{S_e^2 \alpha^2 R^2} = \frac{3,16 \cdot 10^{-8}}{0,64^2 \cdot 0,8^2 \cdot 50^2}$  1p

$P_{in} = 4,82 \cdot 10^{-11} \text{ W} = -73 \text{ dBm}$  so we have 28 dB link gain (which is maybe unrealistic?)

This power needs to be delivered to fiber by RF-transmitter. Since down-link RF-frequency is 900 MHz a transmitter with up-conversion is required. *yes!*



IF-filter  $\left\{ \begin{array}{l} f_c = 100 \text{ MHz} \\ \Delta f = 5 \text{ MHz} \end{array} \right. \Rightarrow \frac{\Delta f}{f} = 5\% \text{ OK!}$   
*required BW*

BPF  $\begin{cases} f_c = 900 \text{ MHz} \\ \Delta f = 100 \text{ MHz} \end{cases}$

Upper sideband used  $f_{RF} = f_{LO} + f_{IF}$   
 Lower sideband at 700 MHz rejected!

With the assumed values and calculations the amplifier need not be there, since enough power is most likely delivered directly from modulator.

Uplink

The mobile phone transmits  $0,7 \text{ W} = 28,5 \text{ dBm}$  with modified Friis eq.  $R_0 = 1 \text{ m}$  and  $N = 2,5$  this yields with  $R = 100 \text{ m}$

$$P_r = P_t \frac{G_t G_r \lambda^2}{(4\pi R_0)^2} \frac{1}{(R/R_0)^N} = 0,7 \cdot \frac{2^2 \cdot 0,35^2}{(4\pi \cdot 1)^2} \cdot \frac{1}{100^{2,5}} = 2,17 \cdot 10^{-8} \text{ W}$$

$f = 850 \text{ MHz} \Rightarrow \lambda = 0,35 \text{ m} \quad G_t = G_r = 2$  (omnidirectional antennas)

$P_r = -46,6 \text{ dBm}$  at access point, the system should also have 20 dB fade margin. Design for  $P_r = -66 \text{ dBm}$

With 20 dB amplification before fiber link  $P_{in} = -46,6 \text{ dBm}$  out fiber.

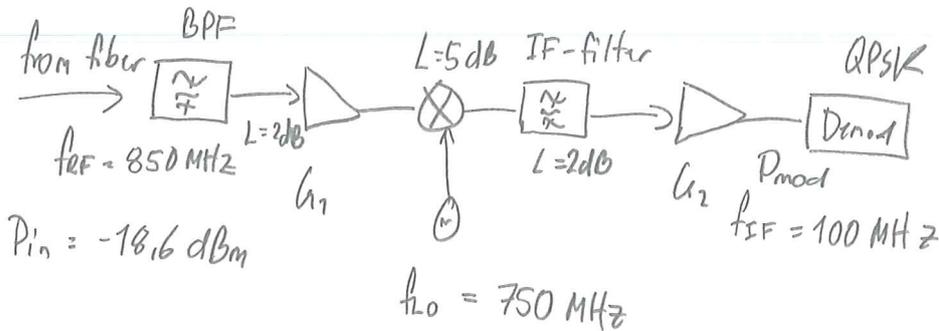
Output power at central unit station after fiber (28 dB gain)

$$P_{out} = P_{in} \alpha^2 R^2 = 2,18 \cdot 10^{-8} \cdot 0,64^2 \cdot 0,8^2 \cdot 50^2 = -18,6 \text{ dBm}$$

This power must be detected by the RF-receiver!  $\lambda = 1500 \text{ nm}$  <sup>+20 Use</sup>

Since a different laser wavelength is used for the up-link (to avoid crosstalk,  $\alpha$  is slightly different and also  $\alpha$  so this is an approximate result)

Use a receiver with a single down conversion step since not very much gain is needed.



Difference frequency is  $f_{IF} = f_{RF} - f_{LO}$   
 Image frequency is at  $f_{IM} = 650 \text{ MHz}$

BPF  $\left\{ \begin{array}{l} f_c = 850 \text{ MHz} \\ \Delta f = 100 \text{ MHz} \end{array} \right. \Rightarrow \text{Image rejected!}$

IF-filter  $\left\{ \begin{array}{l} f_c = 100 \text{ MHz} \\ \Delta f = 5 \text{ MHz} \end{array} \right. \quad \frac{\Delta f}{f} = 5\%$   
 ↑  
 required bandwidth

With filter losses  $2 + 2 \text{ dB} = 4 \text{ dB}$  mixer conversion loss  $5 \text{ dB}$

$\Rightarrow P_{mod} = -18,6 - 4 - 5 + G_{tot}$

Assume  $P_{mod} = 0 \text{ dBm} \Rightarrow G_{tot} = 27,6 \text{ dB}$

can be placed entirely on IF or spread as

$G_1 = 10 \text{ dB} \quad G_2 = 17,6 \text{ dB}$

The design given is for a worst case link from central-unit  $\rightarrow$  access point  
 Should work if used 10 times for 10 access points!